

On the Achievable Rate of a Class of Acoustic Channels and Practical Power Allocation Strategies for OFDM Systems

Yashar M. Aval, Sarah Kate Wilson, *Fellow, IEEE*, and Milica Stojanovic, *Fellow, IEEE*

Abstract—In this paper, we consider a class of single-input–multiple-output (SIMO) underwater acoustic communication channels, where each propagation path can be characterized by a complex-valued Gaussian block-fading model. The capacity of such channels is computed and analyzed using three power allocation strategies: waterfilling, uniform, and ON–OFF uniform power allocation across the signal bandwidth. Our analysis considers the effects of imperfect channel estimation, delayed feedback, and pilot overhead, which are found to contribute to about 1 (b/s)/Hz loss from 4 (b/s)/Hz at 20-dB signal-to-noise ratio (SNR) for the experimental channel. We find that given the long feedback delays associated with acoustic channels, all-ON uniform power allocation, which does not require feedback and is simple to implement, emerges as a justified practical solution that outperforms the other strategies. Furthermore, when considering acoustic-specific propagation effects, such as frequency-dependent attenuation and colored noise, considerable gain can be achieved by selecting the frequency band according to the attenuation pattern and the available transmit power, e.g., at least 6-dB gain for a 10-km link when compared to transmission over a preselected frequency band of 10–15 kHz.

Index Terms—Channel capacity, information rate, lower bound, orthogonal frequency-division multiplexing (OFDM), power allocation, Rician fading, underwater acoustic communications, waterfilling.

I. INTRODUCTION

IN contrast to radio communications, where capacity issues are well understood for point-to-point links (see, e.g., [1] and [2]), the fundamental question of acoustic channel capacity has been an elusive one, mainly because of the lack of well-established statistical channel models. Early work [3] provided a theoretical analysis using time-invariant channel model and focused on low-power applications. The analysis was extended to include a Rayleigh fading channel model in [4], which demonstrated that the channel capacity is limited in that case even if the transmit power is unlimited.

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Y. M. Aval and M. Stojanovic are with Northeastern University, Boston, MA 02115 USA (e-mail: ymaval@gmail.com).

S. K. Wilson is with Santa Clara University, Santa Clara, CA 95053 USA.

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The theoretical work was further advanced in [5] where the channel capacity for multiple-input–multiple-output (MIMO) underwater acoustic channels was studied through decomposing the channel response as the superposition of a time-invariant, and a time-varying, channel. This model is based on the idea that some components of the channel vary slowly over time, and therefore may be assumed known to both the transmitter and the receiver, while the fast channel variations (whose statistics are known to the transmitter) can only be assumed known to the receiver. Kilfoyle *et al.* [5], [6] used experimental data to support this channel model, and showed that spatial modulation can provide up to 5-dB gain compared to temporal modulation only (depending on the channel model).

A similar channel model was used in [7] (both Rayleigh and Rician fading were considered, as well as a model based on experimentally measured scattering function) to analyze the channel capacity and compare it with a lower bound derived for phase-shift keying (PSK) modulation. The analysis in [7] also considered the acoustic-specific frequency-dependent path loss and colored noise, showing that optimal power allocation is based on waterfilling according to the attenuation–noise spectrum if the transmitter only knows the channel statistics.

A Rician channel model has also been used more recently in [8]–[11], where it was supported by experimental measurements. Specifically, Socheleau *et al.* [10] consider a doubly dispersive, wide-sense stationary and uncorrelated scattering (WSSUS) channel, both synthetic and experimental, and specify the channel capacity as a function of the channel scattering function in the presence of intercarrier interference (ICI) and interblock interference (IBI). Motivated by these results, we also use the per-path Rician channel model for the present analysis, and for comparison between simulation and experimental results [12].

Approaching the Shannon channel capacity requires three elements: adaptive power allocation (spectrum shaping), adaptive modulation, and forward error correction (FEC) coding. The effects of power allocation and adaptive modulation on uncoded bit error rate (BER) have been analyzed for underwater acoustic channels in [13], where it was shown that adaptive modulation plays a critical role in achieving a desired BER, and adaptive power allocation reduces the required transmit power noticeably. An alternative, or additional, approach is the use of adaptive FEC coding, which was shown in [14] to be effective in cases when only the signal-to-noise ratio (SNR) information is

fed back to adjust the code rate, while the power and modulation level are kept constant across the carriers.

In this paper, we focus on calculating the ergodic and outage capacity of orthogonal frequency-division multiplexing (OFDM) systems for single-input-multiple-output (SIMO) channels, emphasizing the theoretically achievable rate rather than FEC coding.¹ We show that when considering the short-term channel variations, there is very little difference between waterfilling and uniform power distribution in terms of the achievable rate.

Our present work has four objectives. First, we wish to revisit the fundamental question of acoustic channel capacity and the rate achievable when the channel is not known but only estimated/predicted at the receiver/transmitter. We do so within the framework of OFDM. We perform two types of analysis, one based on the experimental data collected during the 2010 Mobile Acoustic Communications Experiment (MACE'10) [16], and another based on a recently developed channel model [12], where each propagation path is described as a non-zero-mean, first-order autoregressive complex-Gaussian random process. Second, we investigate different power allocation strategies based on short-term fading statistics, including: 1) waterfilling; 2) ON-OFF power allocation [17], [18], where power is allocated in equal amounts but only to those carriers whose SNR is above the waterfilling threshold; and 3) all-ON uniform power allocation, where power is allocated equally to all subcarriers. Third, we address the issue of imperfect channel knowledge in light of: a) pilot overhead needed to estimate the channel at the receiver and the associated channel estimation errors; and b) fundamental propagation delay that affects feedback, limiting the transmitter to operate only with outdated channel estimates. Finally, we consider a channel model which includes acoustic-specific propagation with frequency-dependent attenuation and colored noise. In this case, we introduce two new power allocation strategies: waterfilling based on the attenuation-noise profile only, and uniform power allocation, but across a favorable frequency band only. We show that judicious power allocation based on acoustic propagation effects can increase the data rate and is robust in the presence of delay and channel estimation errors. Our results reflect the actual throughput after taking the guard intervals and pilot overhead into account.

The paper is organized as follows. In Section II, we formally define the power allocation strategies, their respective capacities, and the corresponding lower bounds on the mutual information rate achievable in the presence of channel estimation errors (to which we briefly refer as “rate”). In Section III, we discuss channel estimation and feedback strategies, and the impact of delay. We extend the findings to channels with frequency-dependent attenuation in Section III-C. Section IV is devoted to numerical results that quantify the achievable rate for the considered class of acoustic channels. Conclusions are summarized in Section V.

¹Given the limitation on the length of codewords, there will be a sacrifice on the achievable rate (e.g., see [15] for bounds on applicable code rates when codeword length is limited).

II. ACHIEVABLE RATE

We consider a channel with M receiver elements described by the instantaneous transfer functions $H^1(f), \dots, H^M(f)$, whose values at carrier frequencies $f_k = f_0 + k\Delta f, k = 0, \dots, K-1$ are denoted by $H_k^m = H^m(f_k)$ and assumed to be constant over a subband of width $\Delta f = 1/T$. Defining the vector of channel responses $\mathbf{H}_k = [H^1(f) \dots H^M(f)]^T$, and assuming that the channel variations during the signaling interval T are insignificant, the signal received on the k th carrier frequency is modeled as

$$\mathbf{y}_k = \sqrt{P_k} \mathbf{H}_k d_k + \mathbf{z}_k \quad (1)$$

where P_k is the power allocated to the k th carrier, d_k is the unit-variance information symbol transmitted on this carrier, and $\mathbf{z}_k$ is zero-mean, circularly symmetric Gaussian noise of variance $\sigma_{z_k}^2$ for each receiver element. The noise is assumed to be independent across the receiver elements.² The total power allocated to the system is P_{tot} , and the total bandwidth is $B = K\Delta f$.

The capacity of this system is given by (see [2] for details)

$$C = \Delta f \sum_{k=0}^{K-1} \log_2 \left(1 + \frac{P_k \|\mathbf{H}_k\|^2}{\sigma_{z_k}^2} \right) \text{ (b/s)} \quad (2)$$

where $\|\cdot\|$ denotes the L_2 -norm of a vector. Note that this capacity results from maximum ratio combining (MRC) at the receiver. The capacity can also be expressed as C/B in bits per second per hertz [(b/s)/Hz].

The power allocation policy which maximizes the capacity is specified by the waterfilling rule

$$P_k = \begin{cases} \nu - \frac{\sigma_{z_k}^2}{\|\mathbf{H}_k\|^2}, & \text{when } \|\mathbf{H}_k\|^2 > \frac{\sigma_{z_k}^2}{\nu} \\ 0, & \text{otherwise} \end{cases}, \quad k = 0, \dots, K-1 \quad (3)$$

where the parameter ν is determined such that

$$\sum_{k=0}^{K-1} P_k = P_{\text{tot}}. \quad (4)$$

The power allocation used here requires both the transmitter and the receiver to know the channel. In practice, estimates $\hat{\mathbf{H}}_k$ can be formed at the receiver and passed back to the transmitter, where they are used to implement a power allocation policy. We will consider two such policies: one based on waterfilling, and another based on an *ad hoc* “ON-OFF” rule. In both cases, channel estimation is accomplished using known pilot symbols, for which K_p carriers are reserved in advance. The remaining $K - K_p$ carriers are used for data (information), and indexed by the set $\mathcal{K}_d$. Setting aside a fraction α of the total power for the pilots, $(1 - \alpha)P_{\text{tot}}$ is left for distribution across the data carriers. The two power allocation policies are specified below.

²If the receiver elements are too closely spaced, such that the noise is correlated with some correlation matrix $\mathbf{R}_N$, we can whiten it by premultiplying the received signal with $\mathbf{R}_N^{-1/2}$.

TABLE I
TIME TABLE OF THE ACTUAL CHANNEL, RECEIVER ESTIMATES AND PREDICTED VALUES, AND FEEDBACK INFORMATION
USED AT THE TRANSMITTER FOR POWER ALLOCATION

time [OFDM blocks]	0	1	2	3	4	5	6	7	8
actual instantaneous channel	$\mathbf{H}_k(0)$	$\mathbf{H}_k(1)$	$\mathbf{H}_k(2)$	$\mathbf{H}_k(3)$	$\mathbf{H}_k(4)$	$\mathbf{H}_k(5)$	$\mathbf{H}_k(6)$	$\mathbf{H}_k(7)$	$\mathbf{H}_k(8)$
channel estimate from pilots	$\hat{\mathbf{H}}_k(0)$	-	-	$\hat{\mathbf{H}}_k(3)$	-	-	$\hat{\mathbf{H}}_k(6)$	-	-
channel estimate at the receiver ($D_r = 1$)	$\check{\mathbf{H}}_k(0)$	$\check{\mathbf{H}}_k(1)$	$\check{\mathbf{H}}_k(2)$	$\check{\mathbf{H}}_k(3)$	$\check{\mathbf{H}}_k(4)$	$\check{\mathbf{H}}_k(5)$	$\check{\mathbf{H}}_k(6)$	$\check{\mathbf{H}}_k(7)$	$\check{\mathbf{H}}_k(8)$
channel estimate at the transmitter ($D_t = 4$)	-	-	-	-	$\hat{\mathbf{H}}_k(0)$	$\hat{\mathbf{H}}_k(0)$	$\hat{\mathbf{H}}_k(0)$	$\hat{\mathbf{H}}_k(3)$	$\hat{\mathbf{H}}_k(3)$

A. Imperfect Waterfilling

Power is allocated to the data carriers according to the rule (3), but with channel estimates $\hat{\mathbf{H}}_k$ replacing the unknown values $\mathbf{H}_k$

$$P_k = \begin{cases} \nu - \frac{\sigma_{z_k}^2}{\|\hat{\mathbf{H}}_k\|^2}, & \text{when } \|\hat{\mathbf{H}}_k\|^2 > \frac{\sigma_{z_k}^2}{\nu} \\ 0, & \text{otherwise} \end{cases}, \quad k \in \mathcal{K}_d \quad (5)$$

and the water level ν is determined such that

$$\sum_{k \in \mathcal{K}_d} P_k = (1 - \alpha)P_{\text{tot}}. \quad (6)$$

Note that waterfilling may render some carriers with no power. These are the carriers whose frequencies are not favored by the channel. We refer to them as “bad carriers,” while the remaining carriers that are used to send data are called “good carriers.”

B. ON-OFF Uniform Power Allocation

Using the value of ν found under the previous policy, the available power $(1 - \alpha)P_{\text{tot}}$ is allocated in equal amounts P_d to the good carriers, while nothing is given to the bad carriers [17], [18]

$$P_k = \begin{cases} P_d, & \text{when } \|\hat{\mathbf{H}}_k\|^2 > \frac{\sigma_{z_k}^2}{\nu} \\ 0, & \text{otherwise} \end{cases}, \quad k \in \mathcal{K}_d. \quad (7)$$

The bit rate achievable when only the channel estimates are available can be gauged from the lower bound on mutual information [2]³

$$R = \frac{T}{T + T_g} \cdot \Delta f \sum_{k \in \mathcal{K}_d} \log_2 \left(1 + \frac{P_k \|\hat{\mathbf{H}}_k\|^2}{\sigma_{z_k}^2 + P_k \sigma_{\Delta H_k}^2} \right) \quad (8)$$

where $\sigma_{\Delta H_k}^2 = \sigma_{\Delta H_k^m}^2 = E\{|\Delta H_k^m|^2\}$ is the variance of the channel estimation error $\Delta H_k^m = \hat{H}_k^m - H_k^m$ which is assumed to be the same across all receiver elements, and the factor $T/(T + T_g)$ accounts for the multipath guard time T_g inserted between successive blocks of K carriers. The above expression is valid when the channel estimation error is orthogonal to the estimate $\hat{\mathbf{H}}_k$, e.g., when the estimator is a minimum-mean-squared error (MMSE) estimator.

When the channel is randomly varying, so are the capacity C and the rate R . To account for different channel realizations, one

can use the notion of average capacity $\bar{C} = E\{C\}$, or outage capacity $C_{P_{\text{out}}}$, which is defined for a given outage probability P_{out} through $P_{\text{out}} = P\{C \leq C_{P_{\text{out}}}\}$. Similar definitions apply to the average rate $\bar{R}$ and the outage rate $R_{P_{\text{out}}}$.

III. CHANNEL ESTIMATION AND DELAY

For time-varying channels, we distinguish between two effects of delay, one occurring at the receiver and another at the transmitter (outdated feedback). The first effect is present when the receiver does not compute a new channel estimate in every block, but uses one block's estimate to predict the channel for several blocks. This approach may be taken in practice to reduce the total pilot overhead. Delayed feedback causes the transmitter's channel estimate (which is used to allocate the power) to be outdated even if the receiver conveys its instantaneous estimate. Propagation delay thus presents a fundamental limitation, and one expects it to play a dominant role in an acoustic channel due to the low propagation speed.

To specify the rate, let us denote by D_r the number of blocks over which the receiver makes channel predictions (we will assume that predictions are made to the left and to the right of a pilot block, so a total of $2D_r$ predictions are made for each pilot block), and let D_t be the number of blocks involved in the delayed feedback. At the receiver, a new estimate $\hat{\mathbf{H}}_k(n_0)$ is made at times $n_0 = D_r, 3D_r + 1$, etc., while the predictions $\check{\mathbf{H}}_k(n_0 + l)$ are made in between, for $l = -D_r, \dots, D_r$. Hence, $\check{\mathbf{H}}_k(n_0) = \hat{\mathbf{H}}_k(n_0)$ and $\check{\mathbf{H}}_k(n_0 \pm 1)$, etc., are derived from $\hat{\mathbf{H}}_k(n_0)$. The channel estimate $\hat{\mathbf{H}}_k(n_0)$ is also known to the transmitter, but with a delay. The power $P_k(n_0)$ received during the n_0 th block has thus been allocated based on $\hat{\mathbf{H}}_k(n_0 - D_t)$. Note that while the receiver forms a new channel prediction for every block, the transmitter may or may not do the same, i.e., it can either perform MMSE prediction based on the most recent estimate available from feedback, or keep this estimate as is, and use it for power allocation until the next one becomes available. Since MMSE prediction relies on temporal channel correlation, and this correlation decays over time (e.g., exponentially for a first-order autoregressive model), the predicted channel values tend to diminish, putting the transmitter in an SNR-starved strategy mode where all of the power is assigned to only a few carriers. Therefore, we focus on the case where the transmitter assigns power based on the most recent feedback of the receiver's channel estimate. Table I shows the timing for channel prediction at the transmitter and the receiver, reflecting our choice for power allocation at the transmitter.

Looking at a given frame of $2D_r + 1$ blocks, pilots are assigned to the middle block (n_0), while the remaining blocks use all the carriers for data. Channel mismatch is thus due to both

³We will refer to this quantity briefly as “rate.”

the noise-induced estimation error made in the pilot block and the subsequent change in the channel.

From (8), we now have that the rate during a given block is

$$\underbrace{\tilde{R}(n)}_{n=n_0+l} = \frac{1}{T+T_g} \sum_{k \in \mathcal{K}_d(m)} \log_2 \left(1 + \frac{P_k(n) \|\check{\mathbf{H}}_k(n)\|^2}{\sigma_{z_k}^2 + P_k(n) \sigma_{\Delta H_k}^2(l)} \right) \quad (9)$$

where $\sigma_{\Delta H_k}^2(l) = E\{|H_k^m(n_0+l) - \check{H}_k^m(n_0+l)|^2\}$ is the variance of the channel estimation error that contributes to the overall noise, and the set $\mathcal{K}_d(l)$ is the set of data carriers, which equals $\mathcal{K}_d$ when $l=0$, or all the carriers when $l \neq 0$. Averaged over $2D_r+1$ OFDM blocks with a pilot block in the middle, the instantaneous rate is⁴

$$R(n_0) = \frac{1}{2D_r+1} \sum_{l=-D_r}^{D_r} \tilde{R}(n_0+l). \quad (10)$$

This rate is a random variable whose statistics indicate the corresponding outage rate $R_{P_{\text{out}}}$, or average rate $\bar{R} = E\{R(n_0)\}$, taken over multiple channel realizations.

A. Channel Model

To assess the impact of delay on the achievable rate, time evolution of the channel has to be modeled. We focus on a statistical channel model with P propagation paths where the p th path of the m th receiving element is characterized during the n th block by a random gain $h_p^m(n)$ and delay $\tau_p^m(n)$. The corresponding transfer function is

$$H_k^m(n) = \frac{1}{\sqrt{A_k}} \sum_p h_p^m(n) e^{-j2\pi f_k \tau_p^m(n)} \quad (11)$$

where the factor A_k accounts for frequency-dependent attenuation due to energy spreading and absorption. For the moment, we will set $A_k = 1$. In Section III-C, however, we will consider wideband channels in which dependence on A_k will have a significant effect on the achievable rate.

The path gains within each receiver element are modeled as independent, first-order autoregressive processes that obey the following model [12]:

$$[h_p^m(n) - \bar{h}_p^m] = \rho_p^m [h_p^m(n-1) - \bar{h}_p^m] + \sqrt{(1-\rho_p^{m2})} \sigma_{p,m} \chi_p^m(n) \quad (12)$$

where $\bar{h}_p^m = E\{h_p^m(n)\}$ is the mean value of the gain, the variance of the gain is $\sigma_{p,m}^2 = E\{|h_p^m(n) - \bar{h}_p^m|^2\}$, and $\chi_p^m(n) \sim \mathcal{CN}(0,1)$ is the process noise which is uncorrelated with $h_p^m(n-1)$ as well as across m and p . We also assume a normalization of the path gains h_p^m such that $\sum_p (|\bar{h}_p^m|^2 + \sigma_{p,m}^2) = 1$ for $m=1, \dots, M$, which is justified for scenarios where the receiver elements are separated by a few wavelengths, such that fading is independent among them, yet the average field power is similar (with high communication frequencies, this typically corresponds to apertures that are much smaller than the water column). This assumption holds approximately for the experimental data from the MACE'10

experiment which we use in Section IV to discuss the results. Independence of path gains follows from the fact that reflection points at which scattering occurs are sufficiently far apart [12].⁵

The one-step correlation coefficient ρ_p^m is related to the Doppler spread B_p^m of the p th path to the m th receiver element via $\rho_p^m = e^{-\pi B_p^m (T+T_g)}$ [12]. Time evolution of the path delays is modeled as

$$\tau_p^m(n) = \tau_p^m(n-1) - a_p^m \cdot (T+T_g) \quad (13)$$

where a_p^m is the Doppler factor that captures motion-induced time scaling on the p th path to the m th receiver element. Note that our focus is on conventional OFDM systems, in which Doppler scaling results only in channel variation from one block to the next, while intercarrier interference remains negligible. The statistics of the Doppler factor affect the MMSE channel prediction, as we will discuss in Section III-B.⁶

Depending on the particular circumstances, Doppler scaling factors can be treated as deterministic or random, time invariant or time varying, known or unknown. Here, we assume that the residual Doppler factors (after initial resampling) are unknown, independent across paths, and follow a Gaussian distribution. Such an assumption is supported by the fact that the deterministic Doppler scaling due to transmitter/receiver motion may be removed during initial frame synchronization by resampling the received signal, and the residual Doppler is mainly caused by the random variations in the medium.

B. Channel Estimation and Prediction

We assume that the receiver finds the MMSE channel estimate using pilot carriers, and predicts the channel for the OFDM blocks which do not contain pilots. Denoting by $\mathbf{x}_P^m(n_0)$ the input to the m th channel estimator which contains the values $y_k^m(n_0) d_k^*(n_0)$ observed on the P known pilot carriers, the estimate is given by

$$\hat{H}_k^m(n_0) = E\{H_k^m(n_0) \mathbf{x}_P^{mH}(n_0)\} E\{\mathbf{x}_P^m(n_0) \mathbf{x}_P^{mH}(n_0)\}^{-1} \mathbf{x}_P^m(n_0)$$

where $(\cdot)^H$ denotes the Hermitian operator. The variance of the corresponding error is

$$\sigma_{\Delta H_k}^2(0) = E\{|H_k^m(n_0)|^2\} - E\{H_k^m(n_0) \mathbf{x}_P^{mH}(n_0)\} \times E\{\mathbf{x}_P^m(n_0) \mathbf{x}_P^{mH}(n_0)\}^{-1} E\{H_k^{m*}(n_0) \mathbf{x}_P^m(n_0)\}. \quad (14)$$

We assume equispaced pilot carriers, each with equal power. We also assume an MMSE channel estimator. The variance of the resulting channel estimation error can be expressed as (see [19] for details)

$$\sigma_{\Delta H_k}^2(0) = \lambda \frac{L \sigma_{z_k}^2}{\alpha P_{\text{tot}}} \quad (15)$$

⁵Independence of path gains does not imply independence of equivalent sample-spaced taps (an assumption that is often made in the literature, e.g., [1]).

⁶A similar observation is made in [7], where it is shown that for the experimentally measured channel scattering function, the carrier spacing can be selected such that the variance of ICI for frequencies below 30 kHz (after initial resampling) would be smaller than that of the noise, without exceeding the coherence bandwidth of the channel.

⁴An additional loss factor should be included for half-duplex channels.

where $L = BT_{mp}$, T_{mp} is the multipath spread, and $\lambda < 1$ is a scaling constant [19].⁷

Given the channel model specified by (12) and (13), if the Doppler factors a_p^m follow a zero-mean Gaussian distribution with variance σ_a^2 (the same statistics across channel taps and receiver elements), and amplitudes fade at the same rate $\rho_p^m = \rho$, MMSE channel predictions at the receiver are made as (see Appendix A)

$$\hat{\mathbf{H}}_k(n_0 + l) = e^{-|l|\phi^2} (\rho^l (\hat{\mathbf{H}}_k(n_0) - \bar{\mathbf{H}}_k(n_0)) + \bar{\mathbf{H}}_k(n_0)) \quad (16)$$

where $\phi = \pi\sqrt{2}f_k(T + T_g)\sigma_a$, and $\bar{\mathbf{H}}_k(n_0)$ is a vector of length M , whose m th element is $\bar{H}_k^m(n_0) = (1/\sqrt{A_k}) \sum_p \bar{h}_p^m e^{-j2\pi f_k \tau_p(n_0)}$. With equal noise power across carriers, this channel prediction contains an error whose variance is (see Appendix A)

$$\sigma_{\Delta H_k}^2(l) = \rho^{2|l|} e^{-2l^2\phi^2} \sigma_{\Delta H_k}^2(0) + (1 - e^{-2l^2\phi^2}) \sum_p (\bar{h}_p^m)^2 + (1 - \rho^{2|l|} e^{-2l^2\phi^2}) \sum_p \sigma_{p,m}^2. \quad (17)$$

The first term in the above expression reflects the noise-induced channel estimation error made in the pilot block, while the second and third terms reflect the prediction error caused by the channel dynamics.

The variance (17) can be substituted directly into (9) and (10) for the rate. The tradeoff between the number of pilots and the channel estimation errors then becomes clear: as D_r increases, the total overhead decreases (K_p pilots cover $(K - K_p) + 2D_r K$ data carriers), but every new channel prediction, made farther away from the pilot block, brings a stronger error.

C. Frequency-Dependent Attenuation

In wideband underwater acoustic channels, frequency-dependent attenuation represents another source of frequency selectivity. Unlike the multipath, whose structure changes with the motion of the transmitter and the receiver, nominal characteristics of the frequency-dependent attenuation–noise spectrum can be assessed *a priori*. That knowledge can be used at the transmitter to perform spectrum shaping in a manner similar to waterfilling [20].

The key difference between the multipath-induced frequency selectivity and the frequency-dependent large-scale attenuation is that the latter changes much more slowly (or not at all). Referring to the channel model (11), the factor A_k can thus be regarded as a statistical parameter of the channel, and we will consequently refer to the related spectrum shaping as “statistical waterfilling” (for lack of a better term). We also define a second strategy, analogous to uniform power allocation, where the power is allocated uniformly, but only over a limited bandwidth favored by the attenuation–noise profile. We refer to this strategy as bandlimited uniform.

⁷Depending on the channel estimation technique, the estimation error variance may be different, but it will be proportional to (15) regardless of the technique. For example, if the channel impulse response is sparse, the estimation noise can further be reduced to $\lambda J \sigma_{z_k}^2 / \alpha P_{\text{tot}}$, where $J \leq L$ is the number of active channel taps [19].

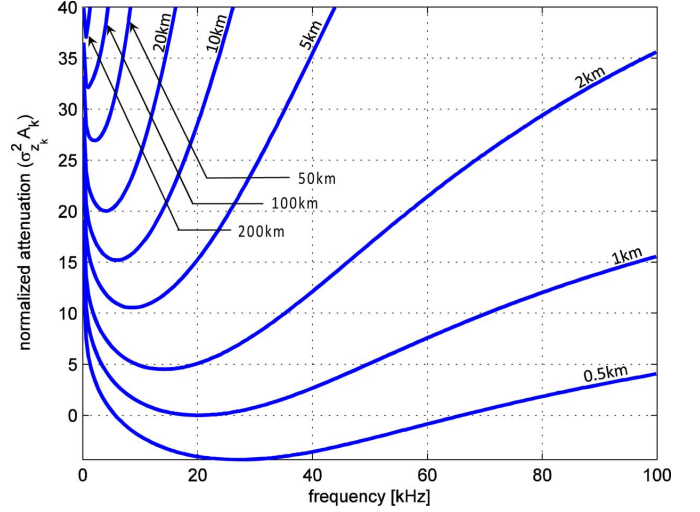


Fig. 1. Frequency-dependent attenuation–noise profile $\sigma_{z_k}^2 A_k$. Normalization is performed such that the 0-dB level corresponds to the minimum point at 1 km. The noise profile is generated as in [20] with the parameters set to no wind ($w = 0$) and moderate shipping activity ($s = 0.5$). The spreading is assumed to be spherical.

Given the parameters A_k and $\sigma_{z_k}^2$, which we assume to be the same for all receiving elements (receiver elements are separated by several wavelengths), statistical waterfilling is applied as follows:

$$P_k = \begin{cases} \nu - \frac{\sigma_{z_k}^2 A_k}{M}, & \text{when } \nu > \frac{\sigma_{z_k}^2 A_k}{M} \\ 0, & \text{otherwise} \end{cases}, \quad k = 0, \dots, K-1 \quad (18)$$

where water level ν is selected as before, according to (4) or (6). This expression is equivalent to the optimal power allocation derived in [7].

The frequency band for bandlimited uniform policy is selected using the value of ν from statistical waterfilling to identify the carriers for which $\nu > \sigma_{z_k}^2 A_k / M$. Power is allocated uniformly to those carriers, while nothing is given to the rest. Fig. 1 illustrates the relevant attenuation–noise characteristic $\sigma_{z_k}^2 A_k$.

IV. RESULTS

Given the candidate power allocation policies, the question arises as to what performance can they deliver in terms of the rate, and how does this performance compare with the channel capacity. On the one hand, we have the imperfect waterfilling which aspires to achieve the optimum (but ignores the penalty of channel estimation errors), while on the other hand, we have ON–OFF power allocation which does not follow any optimization incentive, but is simpler to implement and operate. Finally, we have the unknown-channel feedback-free policy in which power is allocated equally to all carriers.

The results presented below are obtained using simulation and experimental data. The experimental data were recorded in a 100-m-deep, 3–7-km-long mobile channel, with 256 carriers occupying 10–15-kHz acoustic band (for details of deployment, see [16]). The results are based on 1664 OFDM blocks transmitted over a period of 3.5 h. The channel impulse response, estimated for each OFDM block by treating all carriers as pilots, is

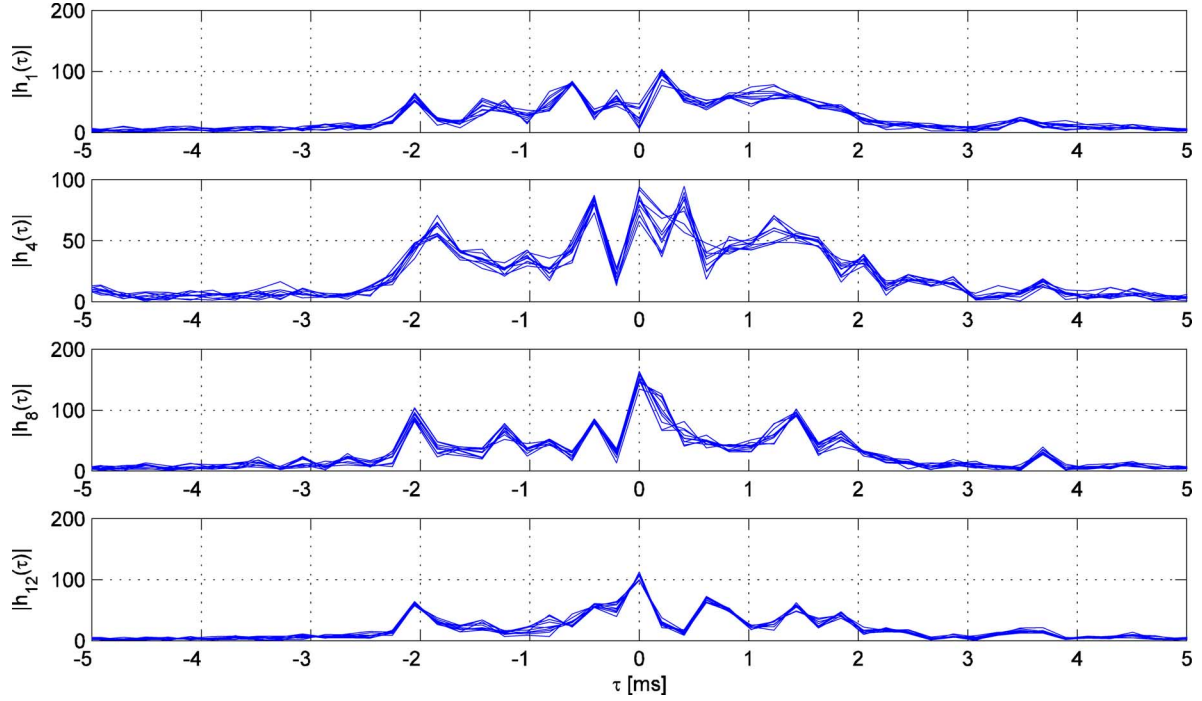


Fig. 2. Ensemble of measured channel impulse responses from ten consecutive OFDM blocks for four receiver elements, demonstrating the evolution of the channel impulse response over time. The length of each OFDM block and the guard interval are 51 and 16 ms, respectively.

taken as the true channel and used for the results corresponding to the perfect channel knowledge. For the rest of the results, a fraction of the carriers are assigned as pilot carriers and artificial noise is added to form the noisy channel estimates. Fig. 2 shows an ensemble of channel impulse responses measured from ten consecutive OFDM blocks.

The guard interval is $T_g = 16$ ms and the block duration is $T = 51$ ms for both the experimental data and the simulation. The simulated channel follows the model of Section III-A, where the average path gains and path delays are selected according to the channel geometry that matches the experimental one.⁸ We select 50 different channel responses (which vary slightly in the placement of transmitter and receiver) and add random time variation over the duration of 100 OFDM blocks (5000 blocks in total). To describe the variation, we use the notion of the average Rician K -factor as introduced in [21], $\bar{K} = \sum_p (\bar{h}_p^m)^2 / \sum_p \sigma_{p,m}^2$, which is assumed to be the same for all receiver elements. The results are based on $K_p = K/8$ channel estimation pilots and pilot power ratio $\alpha = 1/8$, except for the benchmark cases labeled “ideal channel knowledge,” where the channel is assumed to be known to the receiver perfectly and no pilots are needed (data on all carriers).

Fig. 3 shows the cumulative distribution function of the rate (8) calculated using simulated, as well as experimentally measured channels, based on the channel estimation error (15). We

note that the experimental channel matches closely with $\bar{K} = 2$. Different curves on this plot can be used to determine the outage rate for different $\bar{K}$.

Next, we compare the power allocation strategies in terms of the average rate $\bar{R}$ and the outage rate $R_{P_{out}}$. Fig. 4(a) shows $\bar{R}$ and Fig. 4(b) shows $R_{1\%}$ versus SNR, calculated from experimental data. Similar results are obtained in simulation. Different power allocation strategies are seen to perform with negligible difference on this channel, providing about 4 (b/s)/Hz at the SNR of 20 dB under ideal channel knowledge. Channel estimation errors impact all the strategies in a very similar manner, causing a loss of about 1 (b/s)/Hz at 20-dB SNR.

Fig. 5 extends these results to the case of multiple receiving elements for experimental [Fig. 5(a)] and synthetic data [Fig. 5(b)]. The rate now increases linearly with the logarithm of the number of receiver elements, while the loss of rate due to channel estimation errors remains almost unchanged. Similarly, the difference between the average rate and the 1% outage rate remains at about 0.5 (b/s)/Hz regardless of the number of receiver elements.

The benefits of waterfilling and ON-OFF uniform power allocation policies are investigated in Fig. 6(a). This figure shows the increase in rate over that achieved by the uniform power allocation policy $\Delta R/B = R/B - (R/B)_{all-on}$. The maximum gain of 0.15 (b/s)/Hz (and 0.13 (b/s)/Hz for ON-OFF uniform) in the rate occurs at about 0-dB SNR for the single receiving element case ($M = 1$). The gain of waterfilling and ON-OFF uniform power allocation also decreases with multielement combining, but eventually saturates as the aperture remains fixed and the signals received by different elements become correlated. To establish a benchmark, we compare this result to a hypothetical channel [Fig. 6(b)] whose transfer function for each receiver element follows an independent Rayleigh distribution over carriers

⁸The average multipath profile is characterized by the mean gain magnitudes, equal for all receiver elements, β , 0.9β , 0.5β , 0.45β , 0.4β , 0.3β , 0.1β , and nominal delays 0, 0.4, 1.7, 3, 5.5, 7.6, 11.5 ms. The corresponding variances are γ , 0.2γ , 0.5γ , 0.15γ , 0.15γ , 0.07γ , 0.1γ , and the factors β and γ are selected such that the normalization $\sum_p (\bar{h}_p^m)^2 + \sum_p \sigma_{p,m}^2 = 1, m = 1, \dots, M$ is satisfied and the average Rician K -factor $\bar{K} = \sum_p (\bar{h}_p^m)^2 / \sum_p \sigma_{p,m}^2$ equals a desired value. Doppler scaling factors are generated independently for each path and receiver element, as Gaussian distributed with zero mean and standard deviation σ_a which varies between 0 and 5×10^{-5} .

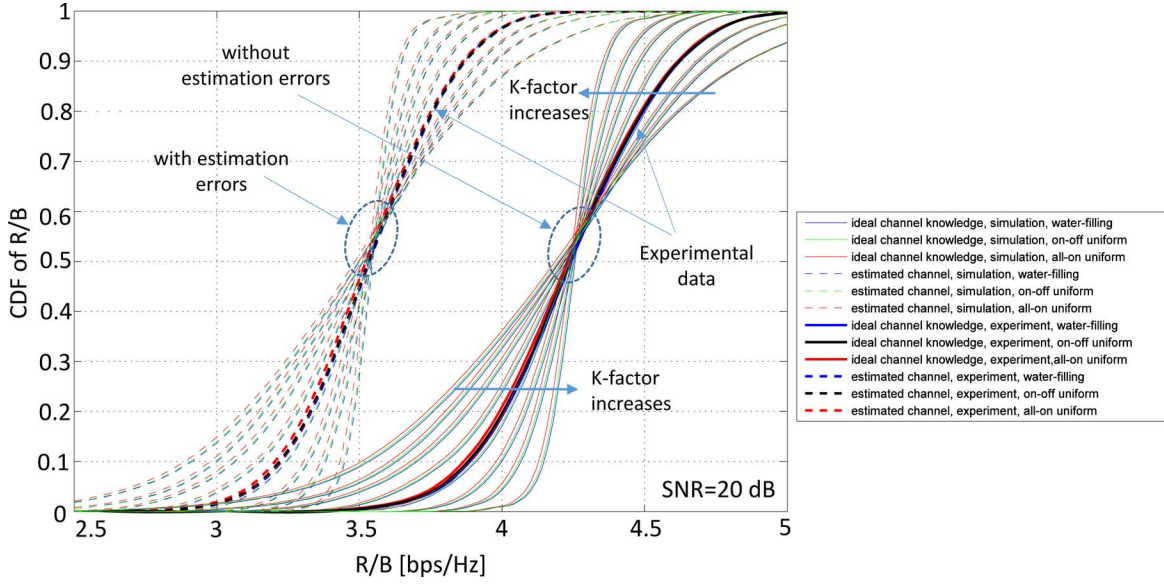


Fig. 3. Cumulative distribution function of the rate (8). The average K -factor takes values 0, 0.5, 1, 2, 4, 8, 16, and 64.

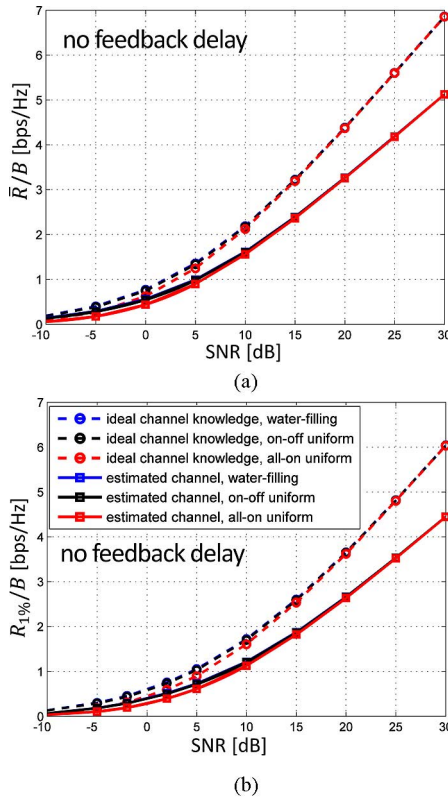


Fig. 4. (a) Average rate and (b) 1% outage rate, calculated using experimental data for single-element receiver. This result corresponds to instantaneous feedback.

$P\{|H_k^m| = x\} = 2xe^{-x^2}$ with $\sigma_{z_k} = 1/\text{SNR}$. Note that this distribution refers to the channel coefficients in the frequency domain, not the time-domain path gains. The M channels are assumed to be independent and MRC is applied at the receiver. The gain of waterfilling for this hypothetical channel closely matches that of the experimental channel for up to four receiver elements, but beyond that, the results differ as the assumption

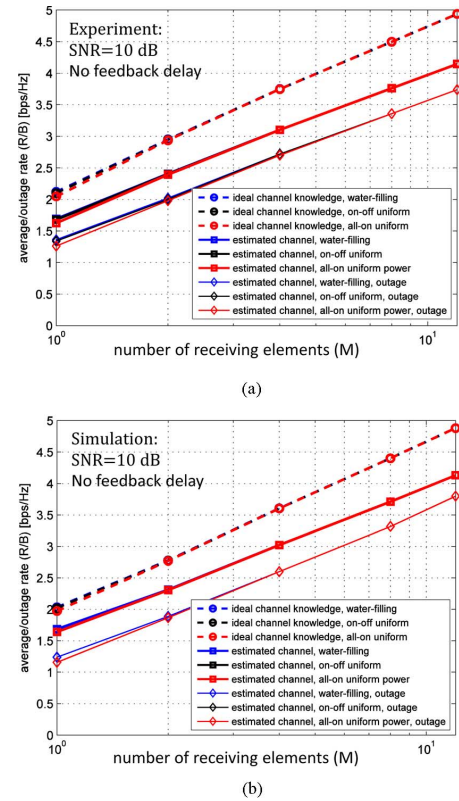


Fig. 5. Average rate calculated using (a) experimental data and (b) simulation versus the number of receiving elements. This result illustrates the effect of noise-induced channel estimation errors, and the difference between average and outage rate. Pilots are inserted into every OFDM block, feedback is assumed to be instantaneous, and the average SNR is 10 dB for each receiver element.

of independence among receiver elements no longer holds for the experiment. Nevertheless, this observation corroborates the general conclusion that the frequency-domain channel coefficients may be modeled as Rayleigh distributed, and that MRC closes the performance gap between uniform power allocation

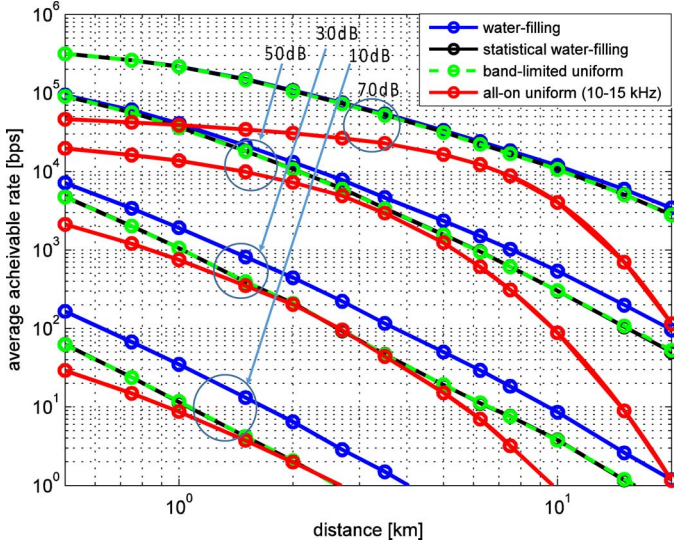


Fig. 8. Average rate versus distance between the transmitter and the receiver for multiple values of transmit power (10, 30, 50, and 70 dB), and four power allocation policies. Channel parameters (A_k and σ_{z_k}) are calculated from Fig. 1. Ideal channel knowledge is assumed both at the transmitter and the receiver, and the all-ON uniform policy is applied across the frequency band 10–15 kHz regardless of the distance and transmit power.

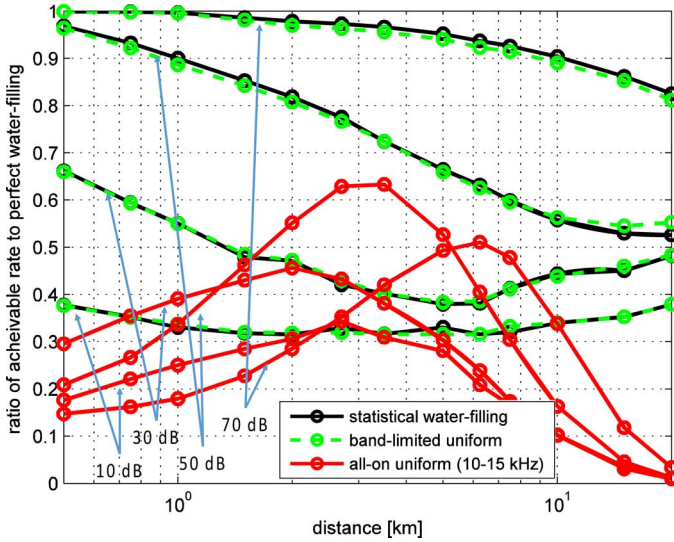


Fig. 9. Ratio of the average rate for statistical waterfilling, bandlimited uniform, and all-ON uniform power allocation policies to waterfilling versus the distance between the transmitter and the receiver. System parameters are the same as in Fig. 8, and ideal channel knowledge is assumed both at the receiver and the transmitter.

Fig. 10 shows a guideline for selecting the optimal frequency band for various distances and transmit powers.

While the results of Figs. 8 and 9 promote application of water-filling in SNR-starved channels, they assume instantaneous feedback. Fig. 11 shows how the benefit of waterfilling vanishes with the introduction of feedback delay. For example, assuming a residual Doppler factor with standard deviation of $\sigma_a = 5 \times 10^{-5}$ (equivalent of motion at the speed of about 0.07 m/s) and one-step correlation coefficient $\rho = 0.8$, and feedback delay as long as 20 OFDM blocks (which is equivalent to the roundtrip propagation delay of a 1-km link), waterfilling is outperformed by the other strategies. The performance of all-ON

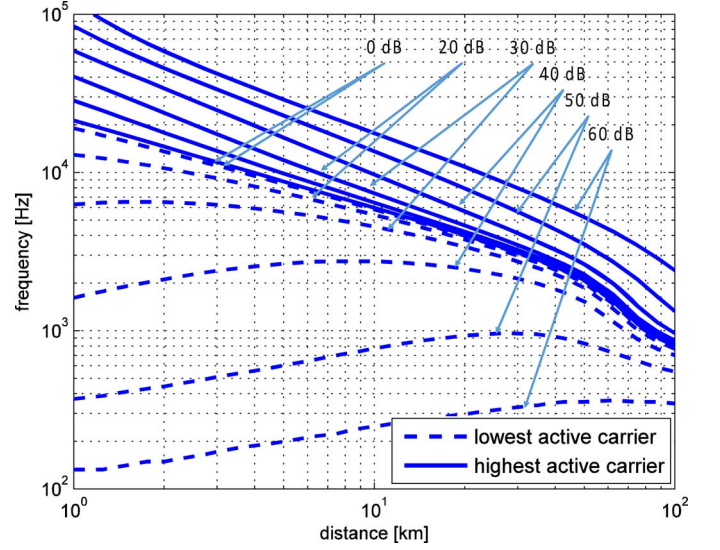


Fig. 10. Optimal frequency band versus distance for different values of transmit power. Bandlimiting is based on large-scale channel parameters (attenuation–noise profile) and the transmitter frequency response is assumed to be flat.

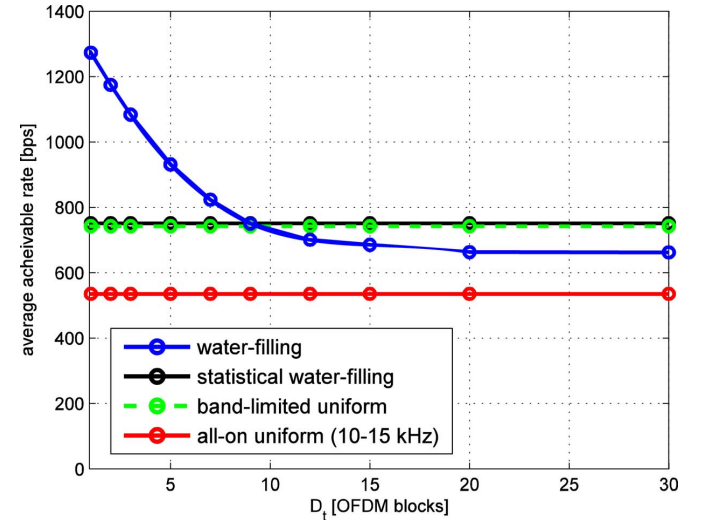


Fig. 11. Achievable rate versus transmitter feedback delay for multiple power allocation policies. Distance between the transmitter and the receiver is 1 km, normalized transmit power is 30 dB, $\rho = 0.8$, and $\sigma_a = 5 \times 10^{-5}$. The receiver is assumed to have ideal channel knowledge (no noise-induced channel estimation error). The rest of the parameters are the same as in Fig. 8.

uniform policy depends on the preselected frequency band. For example, the frequency range between 10 and 15 kHz is a good choice for a 3-km link if an achievable rate of no more than 10 kb/s is desired, while it is far from optimal for higher transmit powers or longer distances.

V. CONCLUSION

A capacity analysis was presented for acoustic channels in which each path is modeled as an autoregressive, non-zero-mean complex-Gaussian process. Numerical results, obtained via simulation and experimentally measured channels, indicate the average achievable rate (lower bound) on the order of 3 (b/s)/Hz at the SNR of 20 dB [1% outage rate is lower by 0.5 (b/s)/Hz] in the presence of channel estimation errors. This achievable rate increases almost linearly with the logarithm of

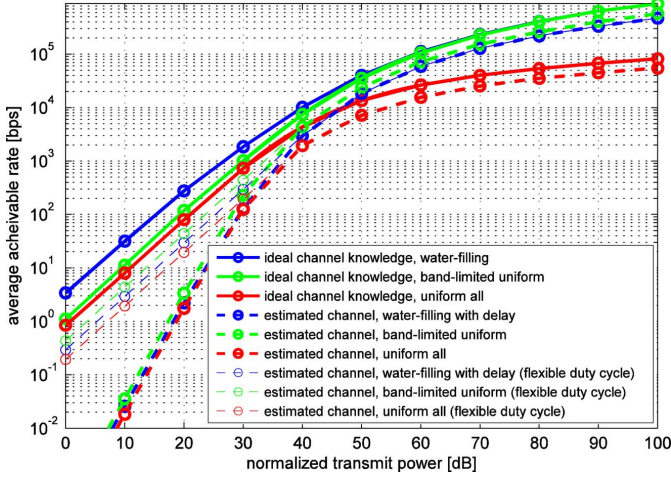


Fig. 12. Achievable rate versus normalized transmit power for estimated channels compared to perfect channel knowledge (distance is 1 km). This figure compares the capacity of estimated channel to the ideal channel knowledge scenario, and also shows that allowing for a flexible duty cycle at the transmitter improves the channel capacity significantly at lower SNRs.

the number of receiver elements. On comparing three power allocation policies—waterfilling, ON-OFF uniform, and all-ON uniform—the first two were found to offer little or no advantage on this channel. The simple, feedback-free policy which does not require any knowledge of the channel and allocates the power uniformly to all the carriers of an OFDM signal thus emerges as a justified choice for practical implementation. Its throughput can be maximized by judicious pilot allocation across blocks that strikes a balance with the channel estimation accuracy which remains the priority of an acoustic receiver.

We also considered the frequency-dependent attenuation profile and colored noise, showing that while uniform power allocation remains the favorable choice, selecting the frequency band based on the channel parameters and available power becomes crucial for optimizing the rate. Future work will address the effect of ICI (with and without ICI mitigation techniques), and long-term channel variation with the attendant methods for rate maximization via power control.

APPENDIX A

MMSE CHANNEL PREDICTION IN PRESENCE OF DOPPLER SHIFTS

This appendix contains the derivation of MMSE channel prediction [see (16)] and the associated prediction error variance [see (17)] based on the channel model introduced by (12) and (13).

To find the MMSE channel prediction for l OFDM blocks into the future (or the past), we need the correlation between $H_k^m(n)$ and $H_k^m(n+l)$

$$\begin{aligned} E\{H_k^m(n+l)H_k^{m*}(n)\} \\ &= E\left\{\sum_p h_p^m(n+l)e^{-j2\pi f_k \tau_p^m(n+l)} \sum_q h_q^{m*}(n)e^{j2\pi f_k \tau_q^m(n)}\right\} \\ &= \sum_p \sum_q E\{h_p^m(n+l)h_q^{m*}(n)\} E\left\{e^{-j2\pi f_k (\tau_p^m(n+l) - \tau_q^m(n))}\right\}. \end{aligned} \quad (19)$$

The first expected value above, $E\{h_p^m(n+l)h_q^{m*}(n)\}$, can be simplified as

$$E\{h_p^m(n+l)h_q^{m*}(n)\} = \bar{h}_p^m \bar{h}_q^{m*} + \rho^l \delta_{p,q} \sigma_{p,m}^2 \quad (20)$$

and the second expected value $E\{e^{j2\pi f_k (\tau_p^m(n) - \tau_q^m(n+l))}\}$ is assumed to be zero for $p \neq q$.⁹ For $p = q$, this expected value is

$$\begin{aligned} E\{e^{-j2\pi f_k (\tau_p^m(n+l) - \tau_p^m(n))}\} \\ &= \int_{-\infty}^{\infty} e^{-j2\pi f_k a_p^m l(T+T_g)} \frac{1}{\sigma_a \sqrt{2\pi}} e^{-(a_p^m)^2 / 2\sigma_a^2} da_p^m \\ &= e^{-(\sqrt{2\pi} f_k l(T+T_g) \sigma_a)^2} \\ &= e^{-l^2 \phi^2} \end{aligned} \quad (21)$$

where the Doppler factors a_p^m are modeled as independent across the paths and receiver elements, and follow a Gaussian distribution with variance σ_a^2 for all paths and receiver elements.

Substituting (20) and (21) into (19), we have

$$E\{H_k^m(n+l)H_k^{m*}(n)\} = e^{-l^2 \phi^2} \sum_p (|\bar{h}_p^m|^2 + \rho^l \sigma_{p,m}^2) \quad (22)$$

where the correlation has two terms, one for the average path gains $\bar{h}_p^m$ and another for the randomly varying part of the path gains, $(h_p^m - \bar{h}_p^m)$, which has the variance of $\sigma_{p,m}^2$. These terms fade at rates $e^{-l^2 \phi^2}$ and $\rho^l e^{-l^2 \phi^2}$, respectively. The correlation (22) suggests the following MMSE prediction:

$$\check{H}_k^m(n+l) = e^{-l^2 \phi^2} (\rho^l (\hat{H}_k^m(n) - \bar{H}_k^m(n)) + \bar{H}_k^m(n)) \quad (23)$$

which can be presented as (16) in vector form. It is straightforward to show that this prediction satisfies the MMSE criterion when $\hat{H}_k^m(n)$ is itself MMSE channel estimate.

The variance of the prediction error is

$$\begin{aligned} \sigma_{\Delta H_k^m}^2(l) &= E\{|\check{H}_k^m(n+l) - H_k^m(n+l)|^2\} \\ &= \rho^{2|l|} e^{-2l^2 \phi^2} E\{|\hat{H}_k^m(n) - H_k^m(n)|^2\} \\ &\quad + (1 - e^{-2l^2 \phi^2}) E\{|\bar{H}_k^m(n)|^2\} \\ &\quad + (1 - \rho^{2|l|} e^{-2l^2 \phi^2}) E\{|H_k^m(n) - \bar{H}_k^m(n)|^2\} \\ &= \rho^{2|l|} e^{-2l^2 \phi^2} \sigma_{\Delta H_k}^2(0) + (1 - e^{-2l^2 \phi^2}) \sum_p (\bar{h}_p^m)^2 \\ &\quad + (1 - \rho^{2|l|} e^{-2l^2 \phi^2}) \sum_p \sigma_{p,m}^2. \end{aligned} \quad (24)$$

Note that since all the receiver elements are assumed to have the same statistics, the right-hand side of the above expression is not a function of m . Therefore, in the text, we omit the superscript m in $\sigma_{\Delta H_k}^2(l)$ for simplicity.

APPENDIX B

FLEXIBLE DUTY CYCLE FOR SNR STARVED CHANNELS

This appendix contains additional results, showing that there is a significant loss in rate due to channel estimation error in low SNR regime, as demonstrated in Fig. 12. One method of

⁹This assumption holds true when the difference between the arrival times τ_p^m and τ_q^m is greater than T/K , which is the case in the majority of practical scenarios.

reducing the estimation error is to transmit at a higher power gP_{tot} for $1/g$ of the time, where $g \geq 1$ is the gain factor. This transmission strategy keeps the average transmit power unchanged while allowing for a degree of freedom in optimizing the tradeoff between the power consumption and the penalty of imperfect channel estimation. Fig. 12 shows that a flexible duty cycle can increase the capacity significantly for channels whose capacity is less than about 5 kb/s (for the distance of 1 km). This observation agrees with the results of [3] where an optimal symbol energy maximizes the rate to power ratio for differentially coherent detection. However, we observe this effect for coherent detection as well which is due to channel estimation errors.

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Yashar M. Aval graduated from the University of Tehran, Tehran, Iran, in 2002 and received the M.S. degree in electrical engineering from Sharif University of Technology, Tehran, Iran, in 2005. Currently, he is working toward the Ph.D. degree in electrical engineering at Northeastern University, Boston, MA, USA.

His research interests include digital communications, orthogonal frequency-division multiplexing (OFDM), underwater acoustic communications, and underwater acoustic networks.



Sarah Kate Wilson (S'91–M'95–SM'99–F'14) received the A.B. degree in mathematics (with honors) from Bryn Mawr College, Bryn Mawr, PA, USA, in 1979 and the Ph.D. degree in electrical engineering from Stanford University, Stanford, CA, USA, in 1994.

She has worked in both industry and academia and has been a Visiting Professor at Luleå University of Technology, Luleå, Sweden; the Royal Institute of Technology, Stockholm, Sweden; and Stanford University. Currently, she is an Associate Professor at Santa Clara University, Santa Clara, CA, USA.

Dr. Wilson has served as an Associate Editor for the IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, the IEEE COMMUNICATIONS LETTERS, and the IEEE TRANSACTIONS ON COMMUNICATIONS. She was the Editor-in-Chief of IEEE COMMUNICATIONS LETTERS. She is the Vice President for Publications of the IEEE Communications Society.



Milica Stojanovic (SM'08–F'10) graduated from the University of Belgrade, Belgrade, Serbia, in 1988 and received the M.S. and Ph.D. degrees in electrical engineering from Northeastern University, Boston, MA, USA, in 1991 and 1993, respectively.

She was a Principal Scientist at the Massachusetts Institute of Technology (MIT), Cambridge, MA, USA, and in 2008, she joined Northeastern University where she is currently a Professor of Electrical and Computer Engineering. She is also a Guest Investigator at the Woods Hole Oceanographic Institution, Woods Hole, MA, USA and a Visiting Scientist at MIT. Her research interests include digital communications theory, statistical signal processing and wireless networks, and their applications to underwater acoustic systems.

Dr. Stojanovic is an Associate Editor for the IEEE JOURNAL OF OCEANIC ENGINEERING and a past Associate Editor for the IEEE TRANSACTIONS ON SIGNAL PROCESSING and the IEEE TRANSACTIONS ON VEHICULAR TECHNOLOGY. She also serves on the Advisory Board of the IEEE COMMUNICATION LETTERS, and chairs the IEEE Ocean Engineering Society's Technical Committee for Underwater Communication, Navigation, and Positioning.